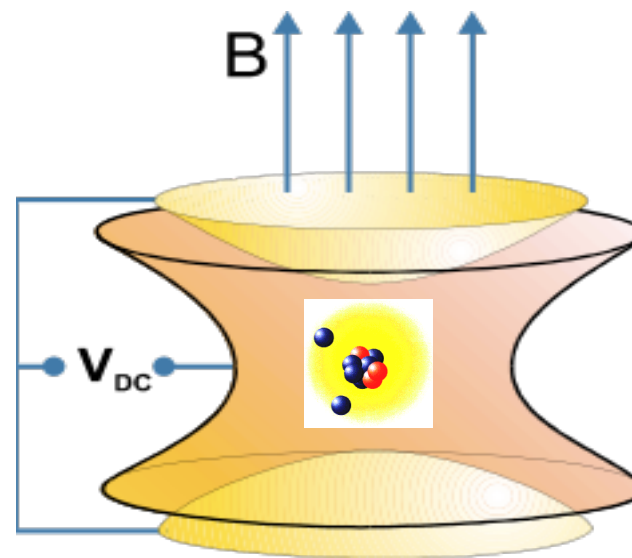


Precision mass measurement of neutron halo nuclei and first radioactive charge-bred ions using the TITAN Penning trap

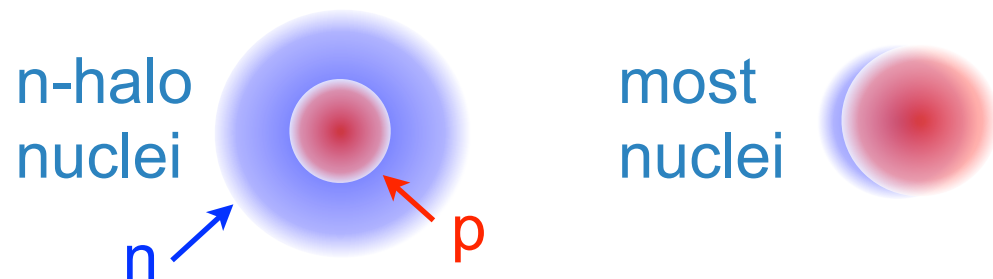


Maxime Brodeur
for the TITAN collaboration



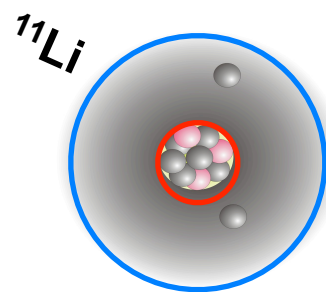
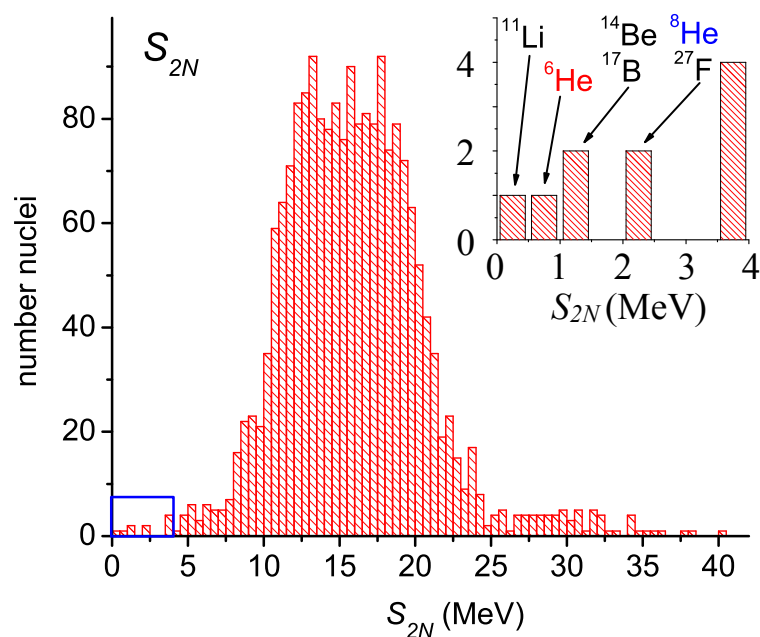
→ Halos are untypical nuclei characterized by:

- **Large** matter distribution (larger than the usual $A^{1/3}$ dependence)
- **Large** difference in charge and matter radii



- **Tiny** one- or two- neutron separation energy

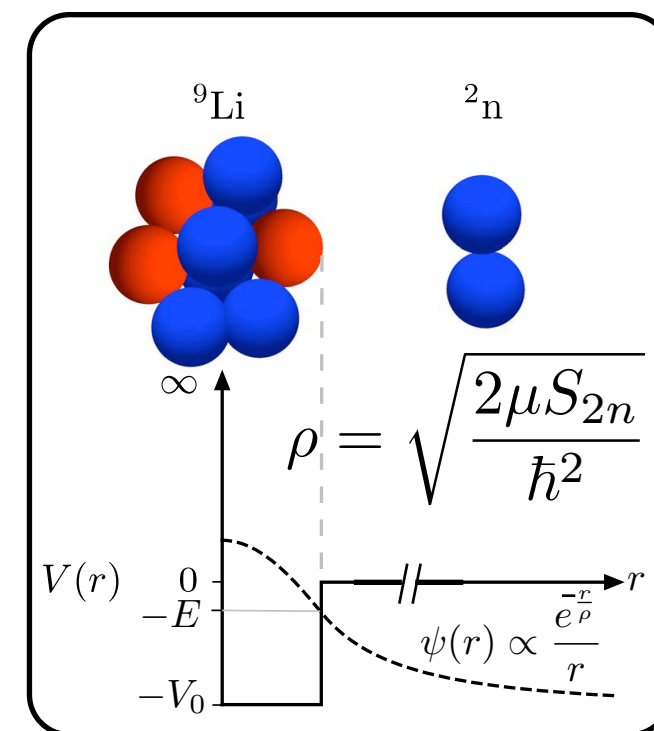
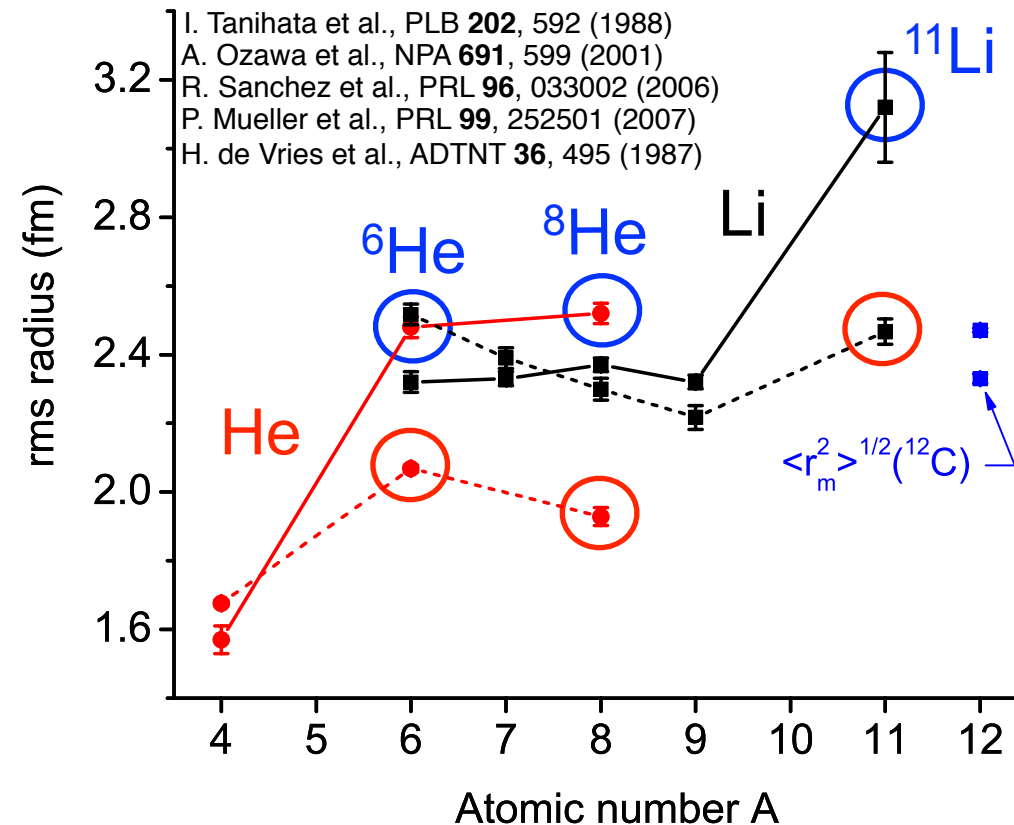
$$S_{xn} = m(Z, N-x) + x m_n - m(Z, N)$$



$$\text{Halo} = R_{\text{Matter}} - R_{\text{Charge}}$$

↑
 S_{2N}

- Hansen & Jonson model for ^{11}Li : ^9Li core + $2n$
- Halo formed by the valence neutrons QM leakage
- S_{2n} regulates extent of halo structure



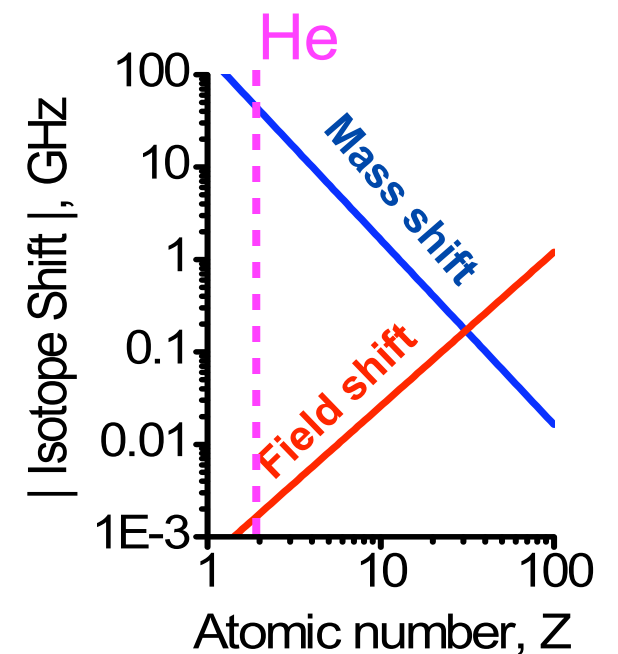
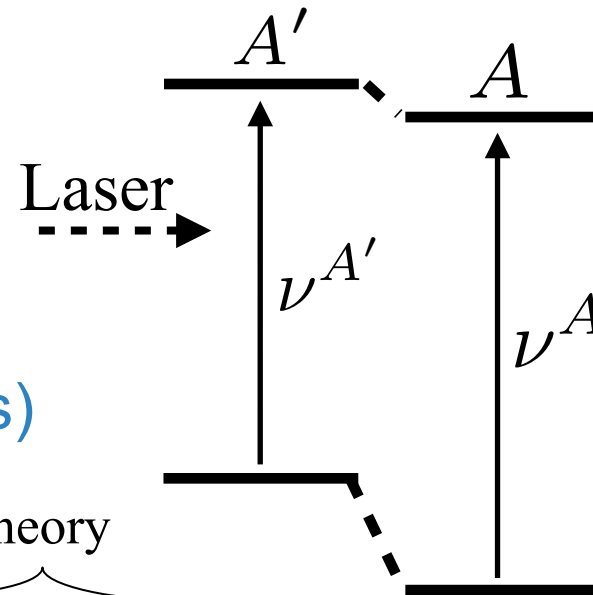
P.G. Hansen and B. Jonson, Europhys. Lett., **4** (4), 409 (1987)

→ The atomic mass is involved in determination of both r_c and S_{2N}

Directly: neutron separation energies

$$S_n = m(Z, N-1) + m_n - m(Z, N)$$

Indirectly: relative charge radius δr_c
determination via isotopic shifts
measurement (of atomic energy levels)



$$\underbrace{\delta\nu^{A,A'}}_{\text{Experiment}} = \nu^A - \nu^{A'} = \underbrace{\delta\nu_{MS}^{A,A'}}_{\text{Mass Shift}} + \underbrace{\delta\nu_{FS}^{A,A'}}_{\text{Field Shift}}$$

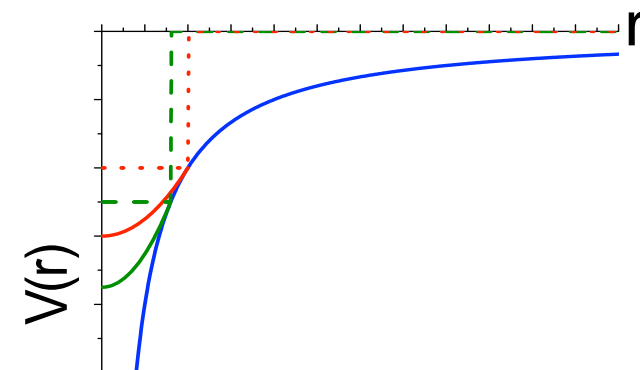
Change in mass of the nucleus $\propto \frac{M_A - M_{A'}}{M_A \cdot M_{A'}}$

Change in nucleus size = $K_{FS} \cdot \delta\langle r_c^2 \rangle^{A,A'}$

This change the nucleus recoils

This change electrical potential

For ${}^8\text{He}$, M.S. 72 000 times larger than F.S.
and needs to be known at same precision



→ Mass is the **major** contribution to the error on ^8He relative charge radius

Error budget on relative charge radii

Error	^6He (%)	^8He (%)
IS Statistical	6	18
Atomic mass	19	58
IS systematics	75	24

Error calculated from: P. Mueller et al., PRL **99**, 252501 (2007)

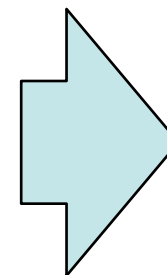
→ Mass precision required < 350 eV for ^6He
 < 730 eV for ^8He

Tabulated mass excesses (M.E. = $m - A$)

Isotope	M.E. (keV)
^6He	$17\,595.11 \pm 0.76$
^8He	$31\,598.0 \pm 6.9$
^8He	$31\,593 \pm 8$
^8He	$31\,613 \pm 17$

G. Audi et al., NPA **729**, 337 (2003)

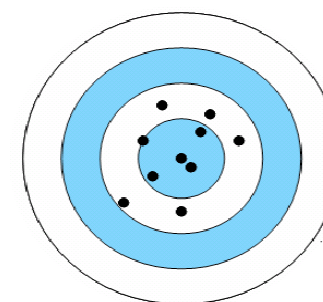
← Need **2x** more **precise**
 ← Need **10x** more **precise**



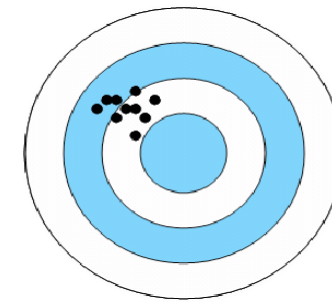
relative uncertainty of $\sim 1 \times 10^{-7}$ on the mass needed

The **two** ^8He measurements **differs** by **20 (19) keV**, which could lead to change in relative charge radius of 40%

... masses also need to be more **accurate!**



accurate, but not precise



precise, but not accurate

Besides metrology, **why** do we need to increase charge radii precision?

- Current **experimental** charge radii are at a similar level of precision as **theory**
- Need more **precise** and **accurate** mass for reliable test of nuclear theory

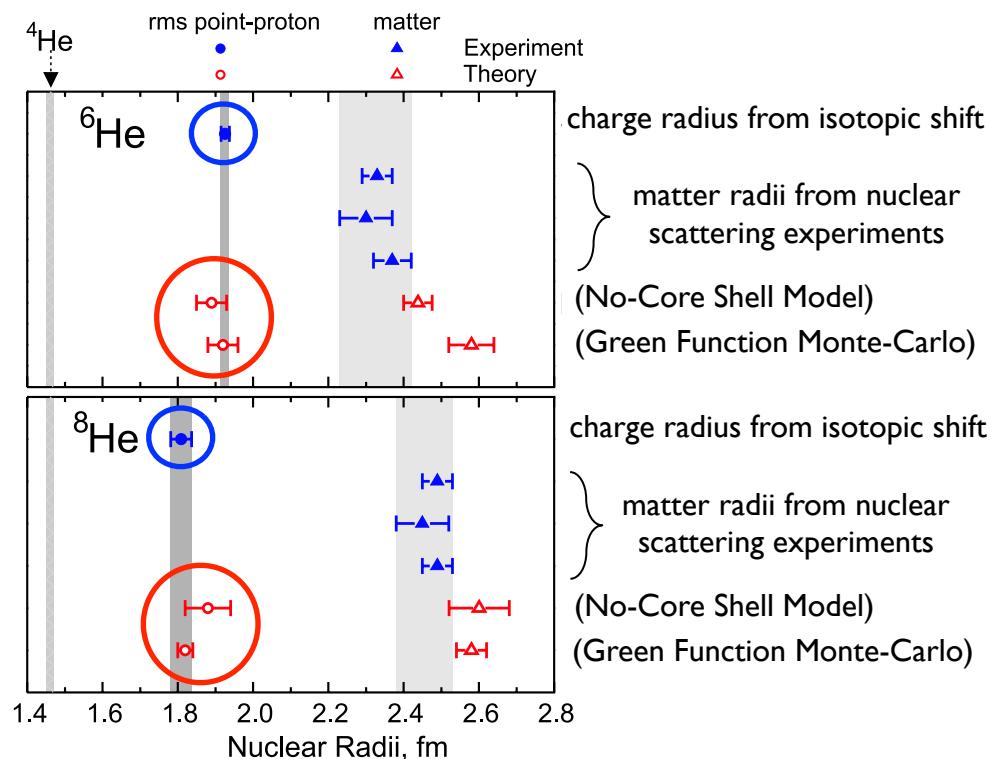
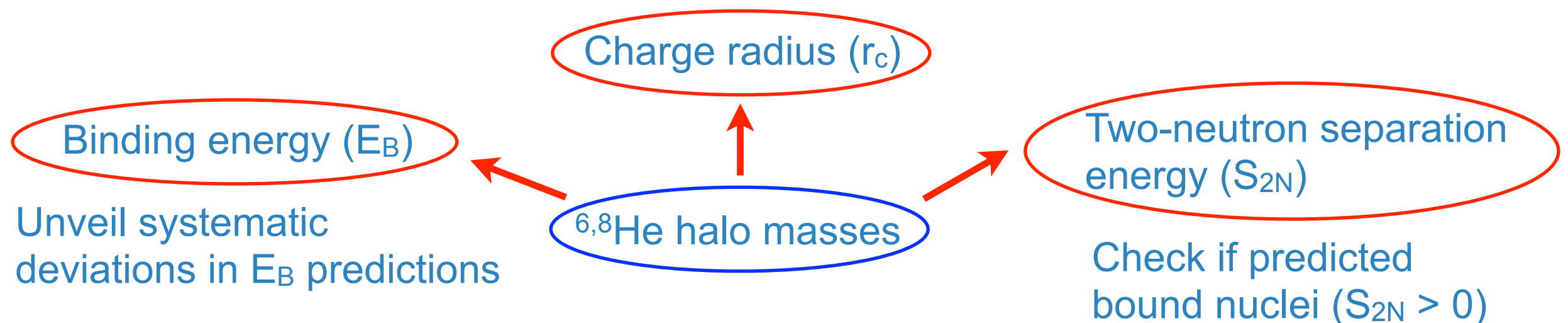
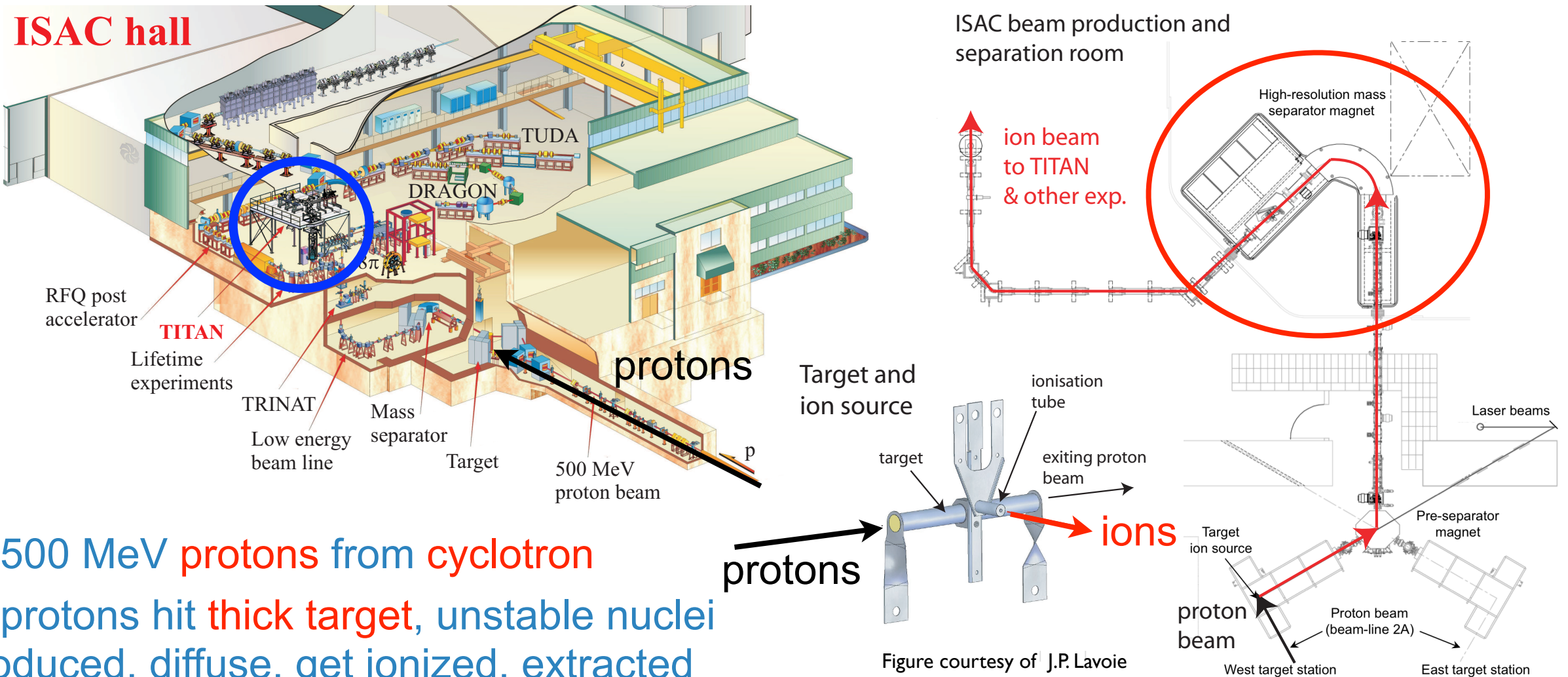


Figure from: P. Mueller et al., PRL **99**, 252501 (2007)

- from Muller et al., ab-initio **theories** charge radius predictions for ${}^6,8\text{He}$ **agree** with value from isotopic shift **measurement**
- Does it still hold using the more accurate & precise values obtained from the TITAN masses?
- How well these methods predicts other observables?



Location of the TITAN Penning trap at the TRIUMF ISAC facility



- 1) 500 MeV protons from cyclotron
- 2) protons hit thick target, unstable nuclei produced, diffuse, get ionized, extracted
- 3) contamination removed using mass separator (resolution: $m/\Delta m = 3000$)

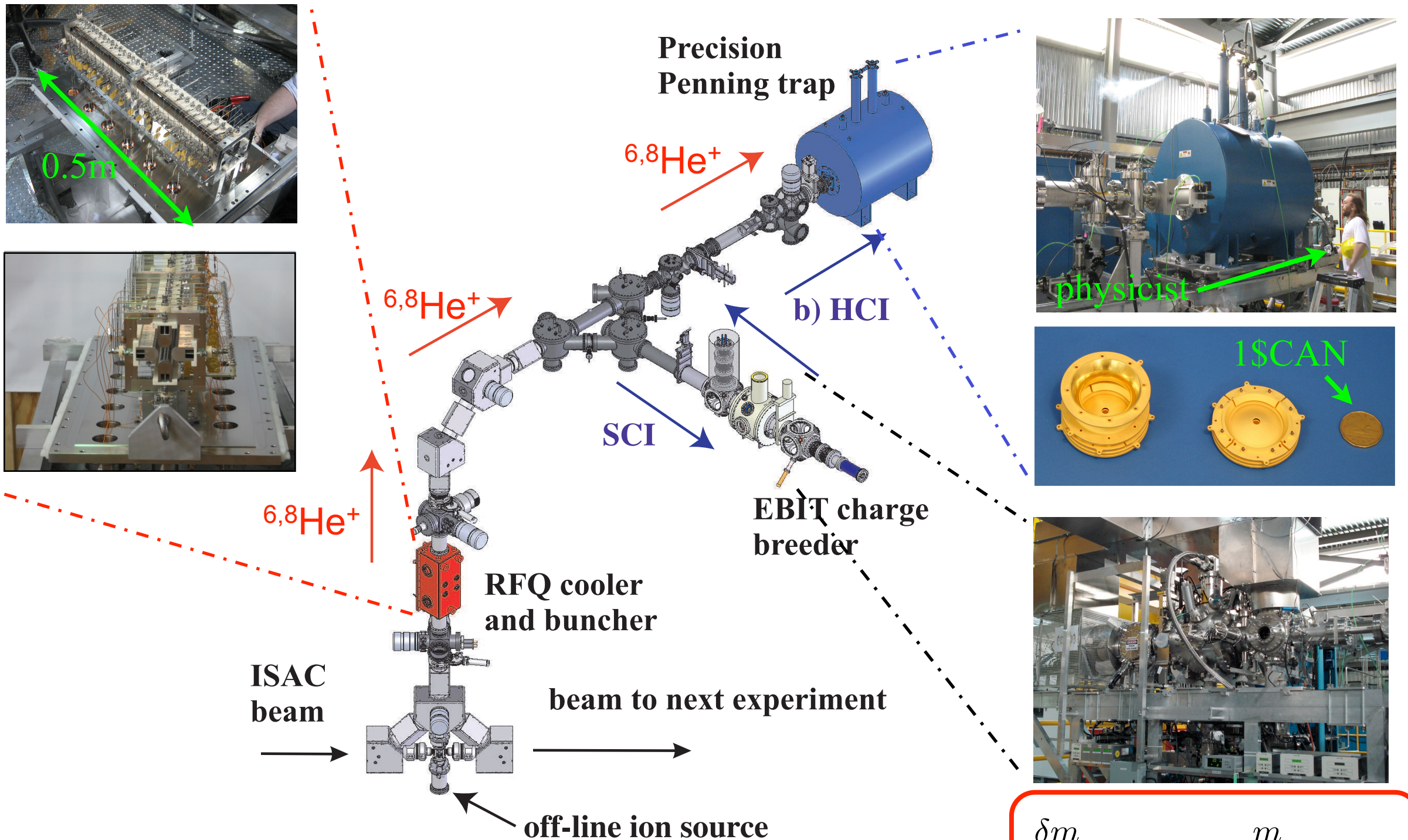
Closest contaminants in mass to ${}^6,8\text{He}$

Isotope	Isotope Δ (keV)	contaminant	cont. Δ (keV)	$m/\Delta m$
${}^6\text{He}$	17 592.09(6)	${}^6\text{Li}$	14 086.88(2)	1600
${}^8\text{He}$	31 609.74(12)	${}^8\text{Li}$	20 945.80(11)	700

(mass excess: $\Delta = m - A$)

→ For all n-halo mass measurement, contamination was resolved

TITAN: TRIUMF Ion Trap for Atomic and Nuclear science



$$\frac{\delta m}{m} \approx \frac{m}{q \cdot B \cdot T_{RF} \cdot \sqrt{N_{ion}}}$$

Depending on the **count rate** and **excitation time**, TITAN Penning trap can achieve **precision** in the **ppb** range for **$A < 10$** .

$$\frac{\delta m}{m} \approx \frac{m}{q \cdot B \cdot T_{RF} \cdot \sqrt{N_{ion}}}$$

- **But** need to determine if the system is also accurate at this level!
- To do so, several sources of systematic errors were investigated, including: (for the **3.6 V trap depth** used for the halo mass measurements)

Recall: $R = \nu_{c,inter} / \nu_c$ $m = \bar{R} \cdot (m_{cal} - m_e + B_{e,cal}) + m_e - B_e$

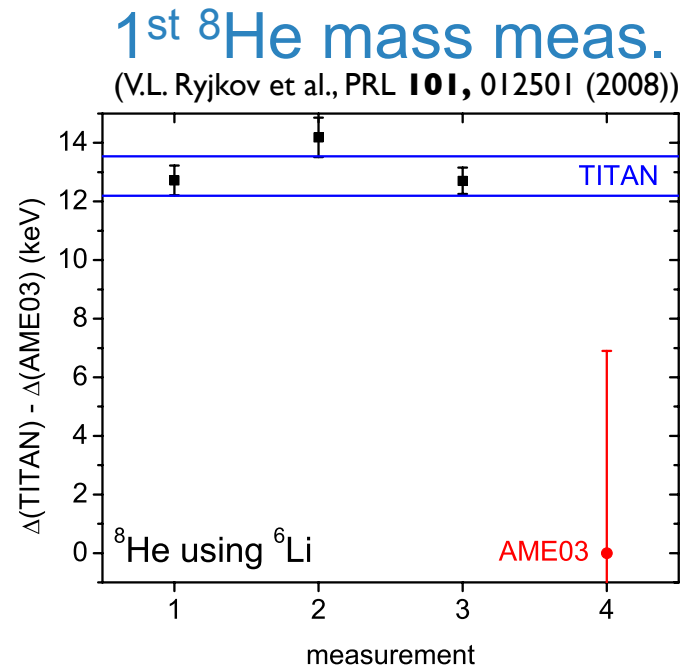
Error	$\Delta R/R (\times 10^{-10})$
magnetic field inhomogeneities	$0.2 \cdot \Delta A$
misalignment and harmonic distortion	$4.2 \cdot \Delta A$
incomplete compensation	$0.5(5) \cdot \Delta A$
non-linear magnetic field fluctuation	$1.5 \cdot \Delta t \text{ (h)}$

(M. Brodeur Ph.D. thesis, UBC (2010))

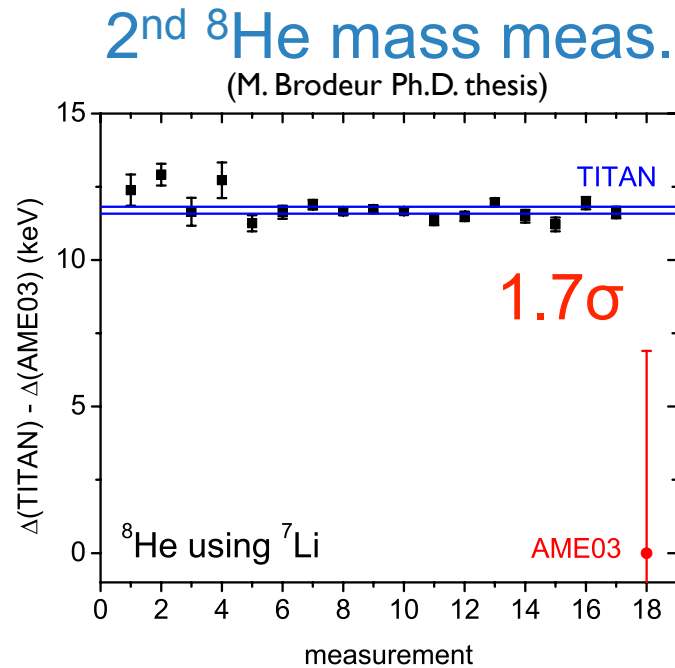
As well as other sources of errors that can be minimized during the measurement:

- Relativistic effects (adjusting ion radius such they have similar velocity)
- Ion-ion interaction (adjust count rate such as to have mainly one ion at the time)

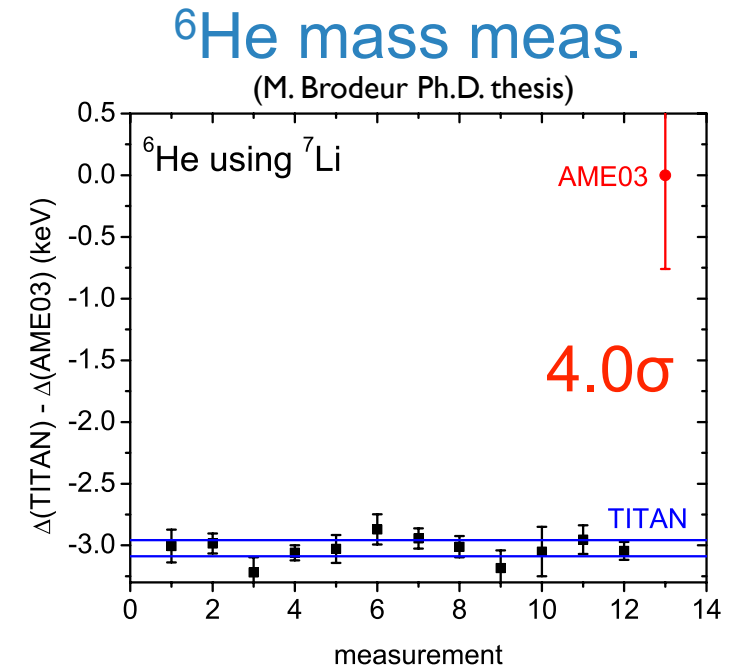
TITAN mass excesses Δ compared to AME03



counts rate: ~ 3 ions/min



~ 40 ions/min



~ 100 ions/min

Error budget (note: trapping potential $V_0 = 3.6\text{V}$)

Error	$\Delta R/R \times 10^{-9}$ (^6He)	$\Delta R/R \times 10^{-9}$ (^8He)
Statistical	4.9	5.9
Ion-ion interaction	8.1	13.3
Total	9.4	14.6

Upper limit on the error due to the interaction between $^6,^8\text{He}$ and ionized background gas.

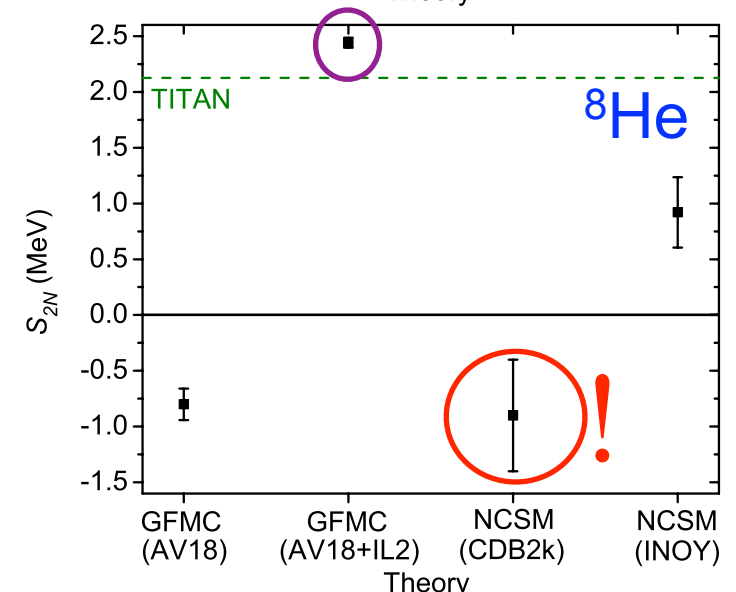
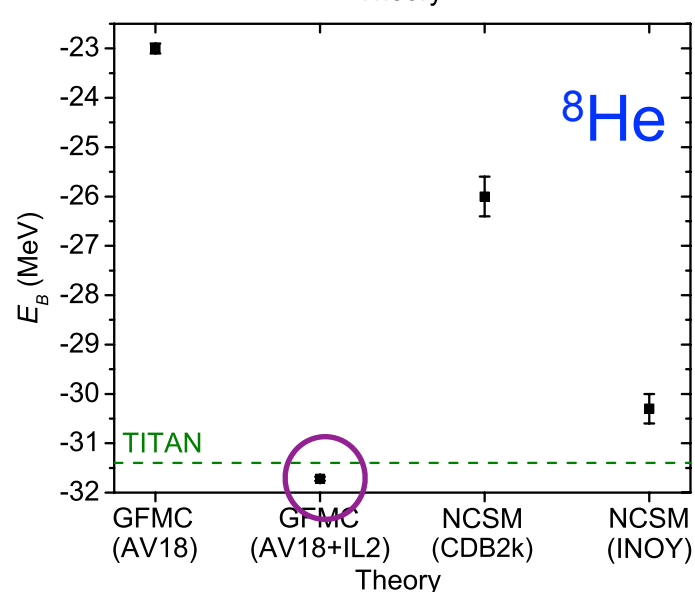
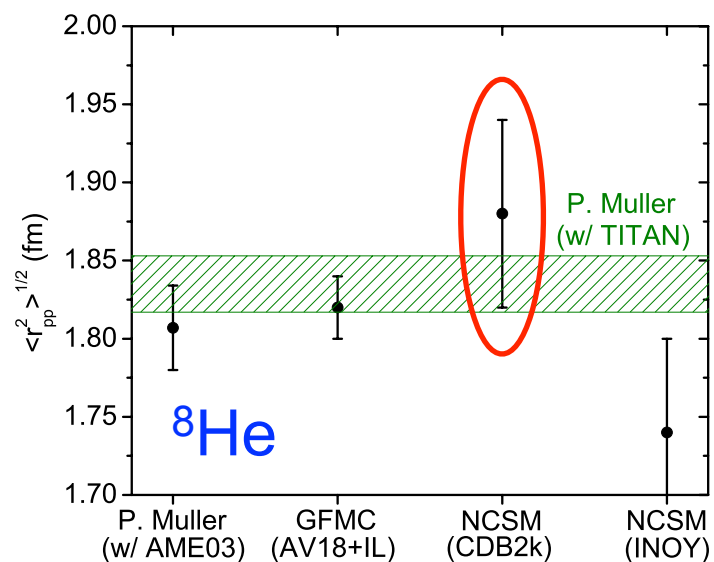
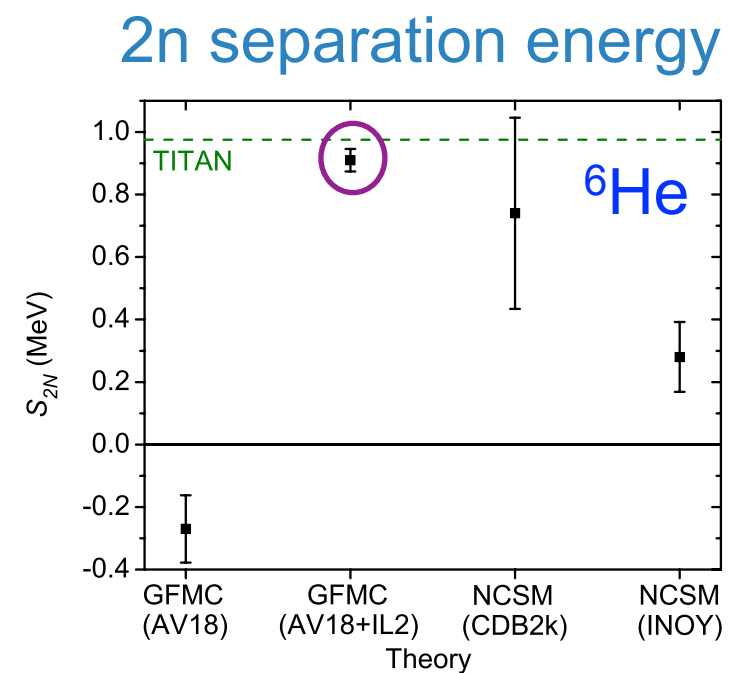
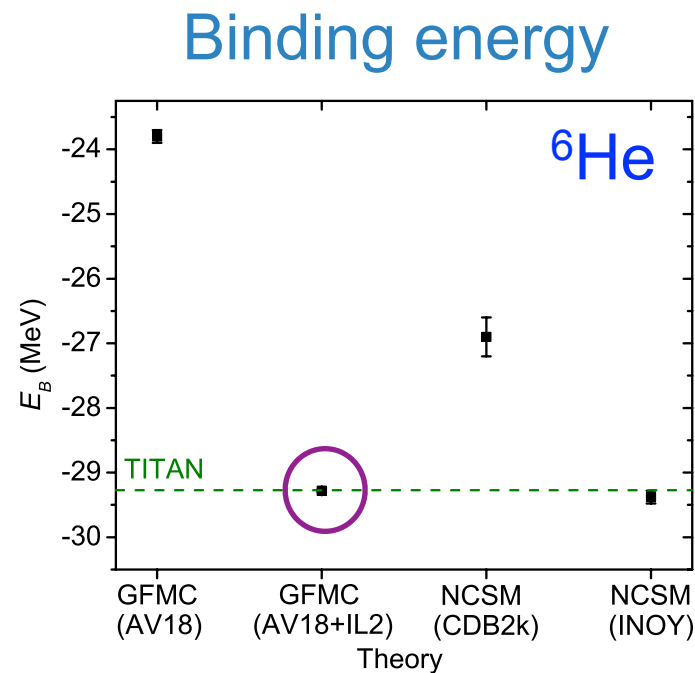
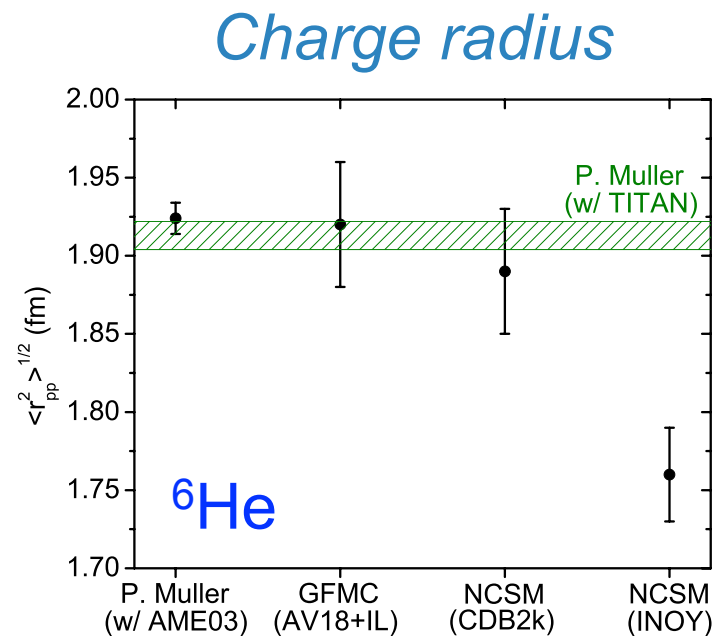
The other sources of systematic errors are < 1 ppb

Accuracy check: mass measurement of ^6Li and ^4He

Isotope	$\Delta(\text{TITAN})$ (keV)	$\Delta(\text{lit.})$ (keV)	$\delta\Delta$ (eV)
^4He	2 424.915(18)	2 424.915 65(6)	-1(18)
^6Li	14 086.867(9)	14 086.881(20)	-14(22)

Both results agrees with literature

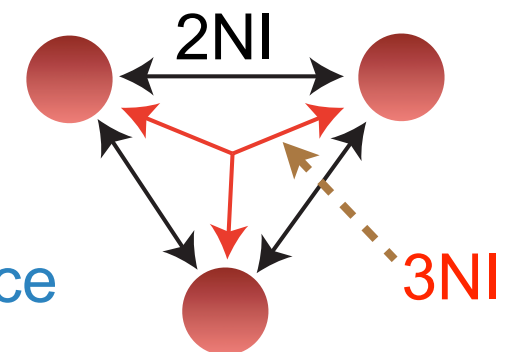
(conservative estimate obtained from count rate analysis)



→ Both the GFMC & NCSM r_c agrees with new exp. ${}^6,8\text{He}$ r_c

GFMC (AV18+IL) → Method that provides the closest values to experiment
Only method that uses 3 nucleons interaction (3NI)

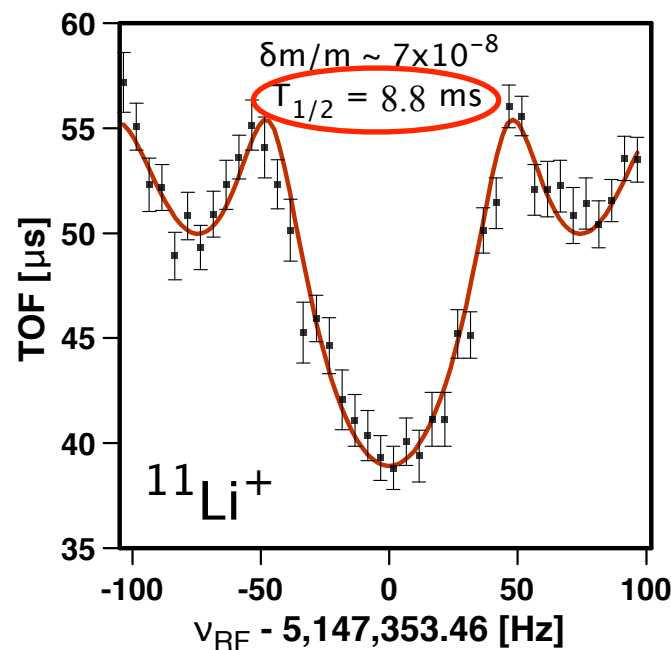
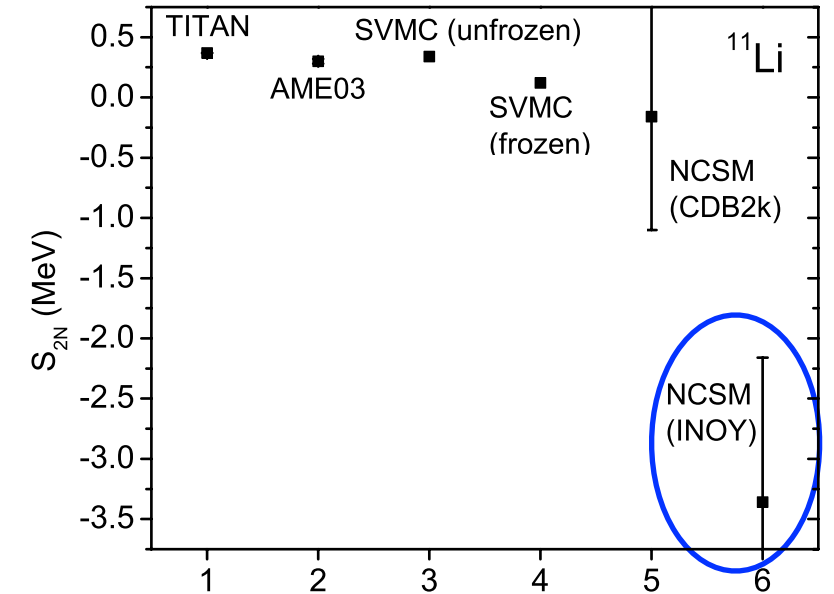
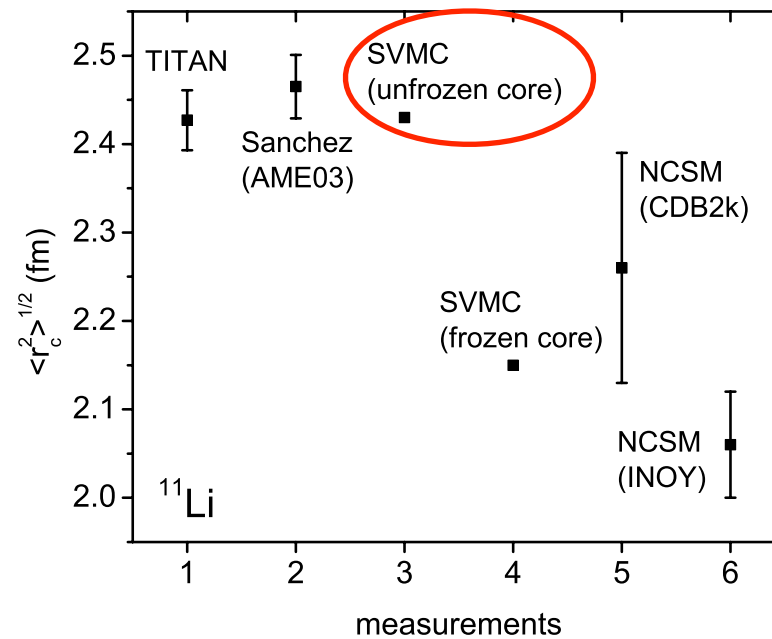
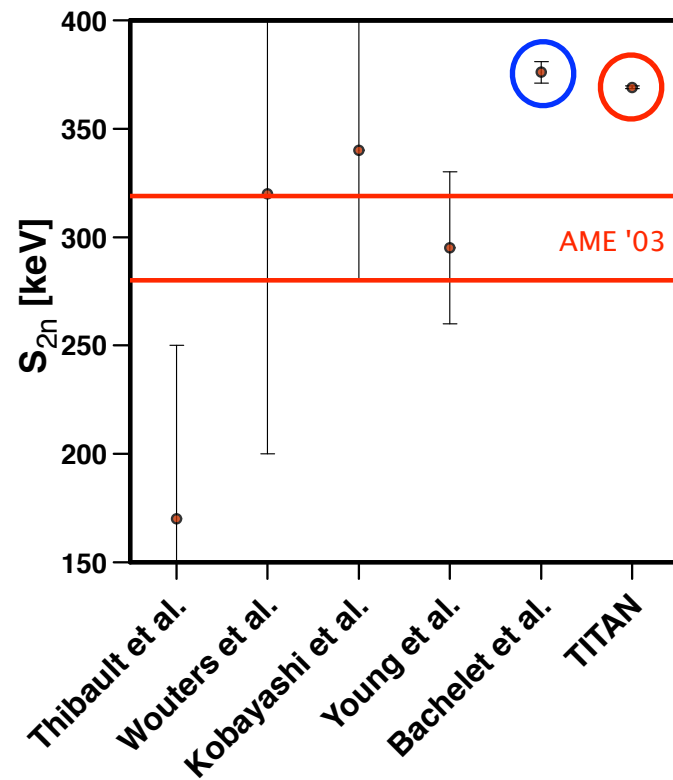
NCSM (CDB2k) → Produce a physical r_c for an unbound nuclei, consequence of using faster Gaussian fall-off and small model space.



Bachelet et al. measurement shows 65 keV deviation with AME03

C. Bachelet et al., Phys. Rev. Lett. 100, 182501 (2008)

Confirmed by the TITAN shortest lived mass measurement using Penning trap

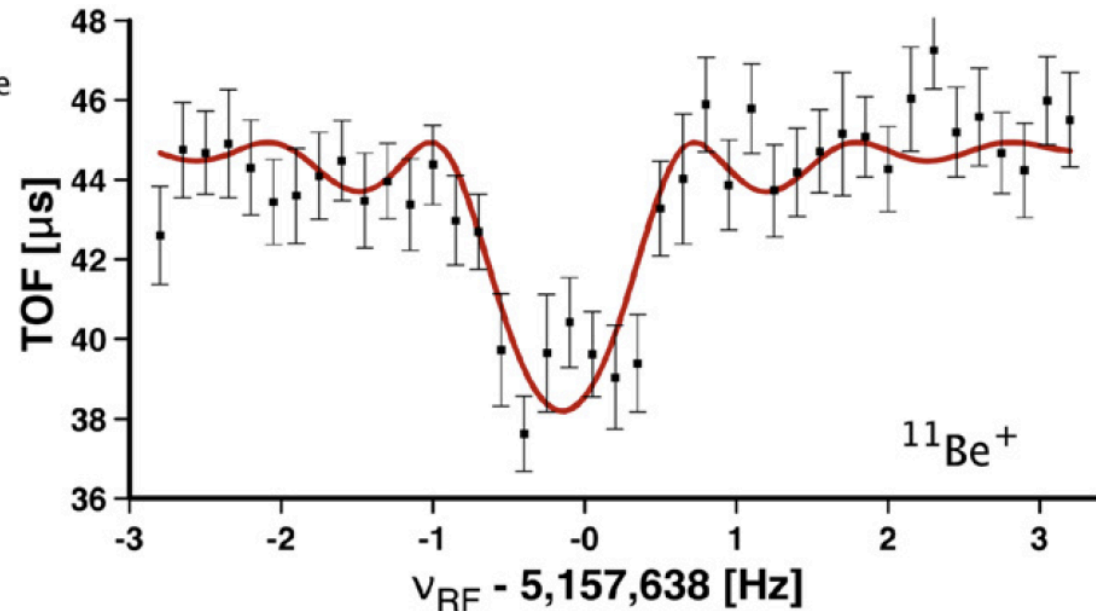
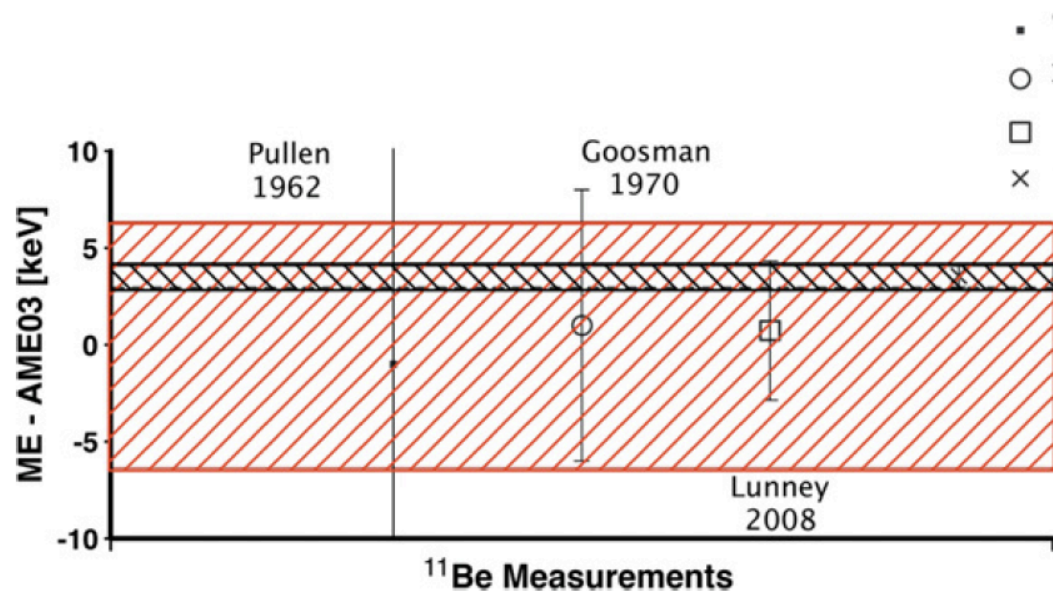


→ NCSM (INOY): unbound ^{11}Li with a physical r_c

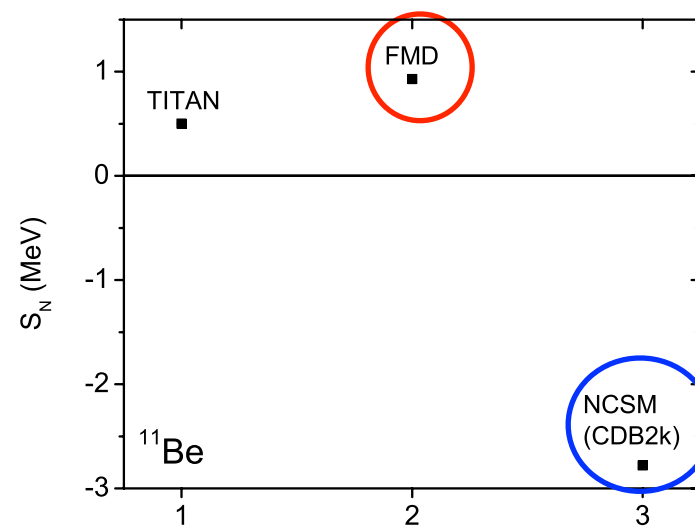
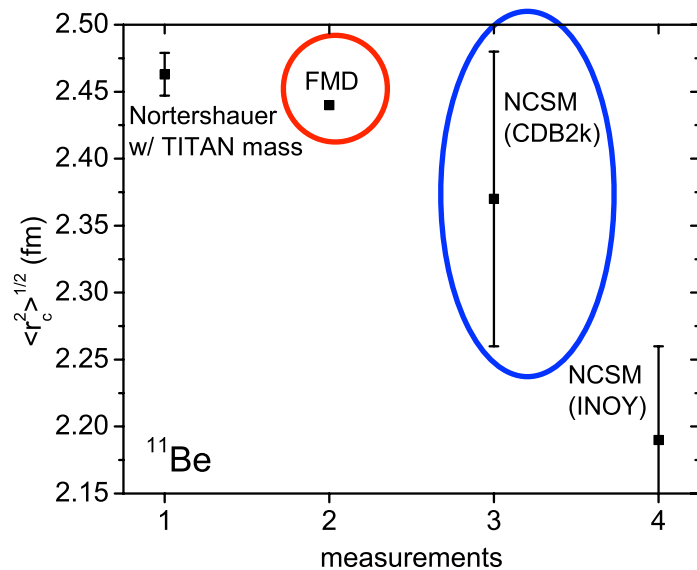
→ Stochastic Variational Monte-Carlo cluster model (SVMC) with unfrozen core gives the best agreement for both r_c and S_{2N}

→ The ^9Li core should be seen as unfrozen, which means it is allowed to be deformed by the presence of the valence neutrons

TITAN mass measurement of the one n-halo ^{11}Be



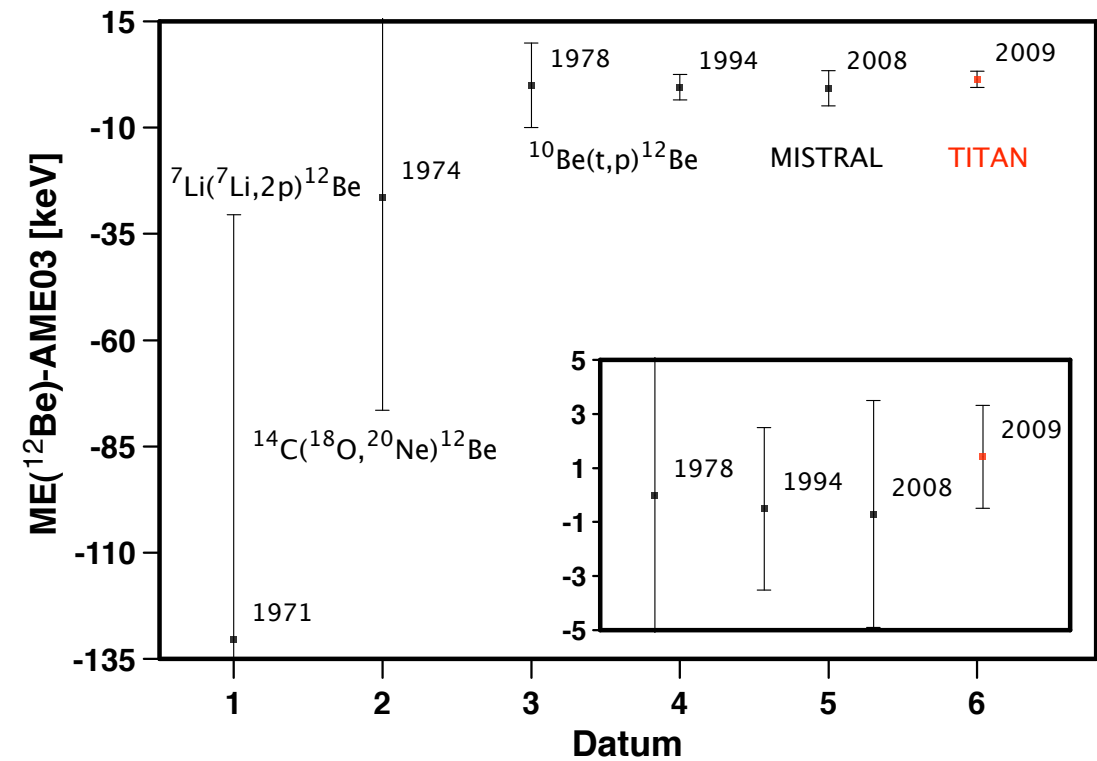
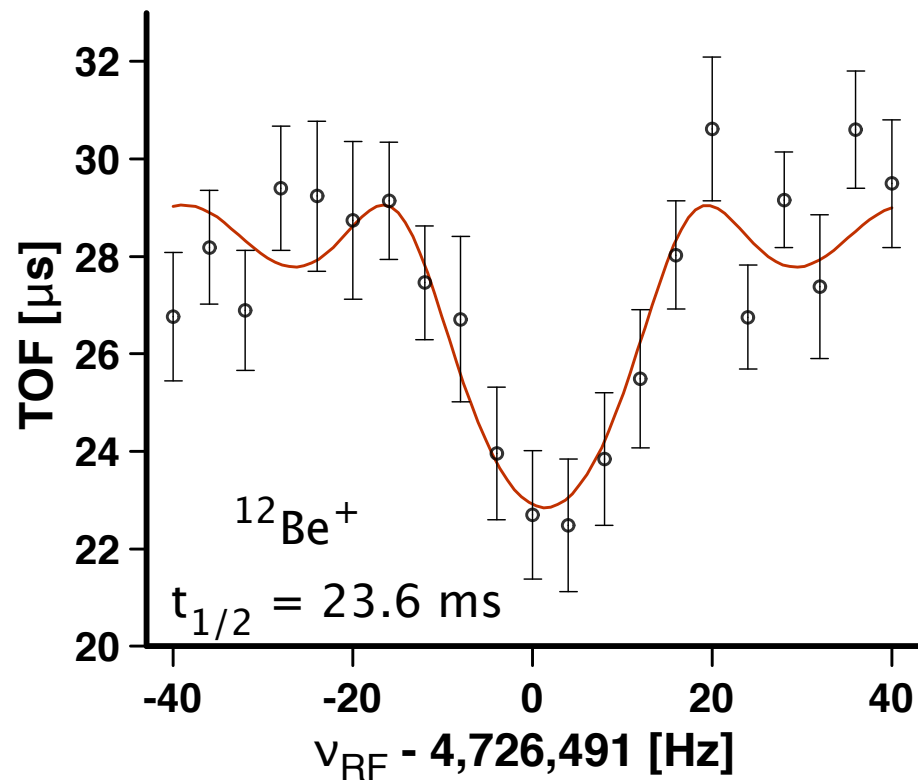
- Improve precision on the mass by one order of magnitude
- The latest charge radius determination uses the TITAN mass
(Nörtershäuser et. al., PRL **102** (2009) 062503)



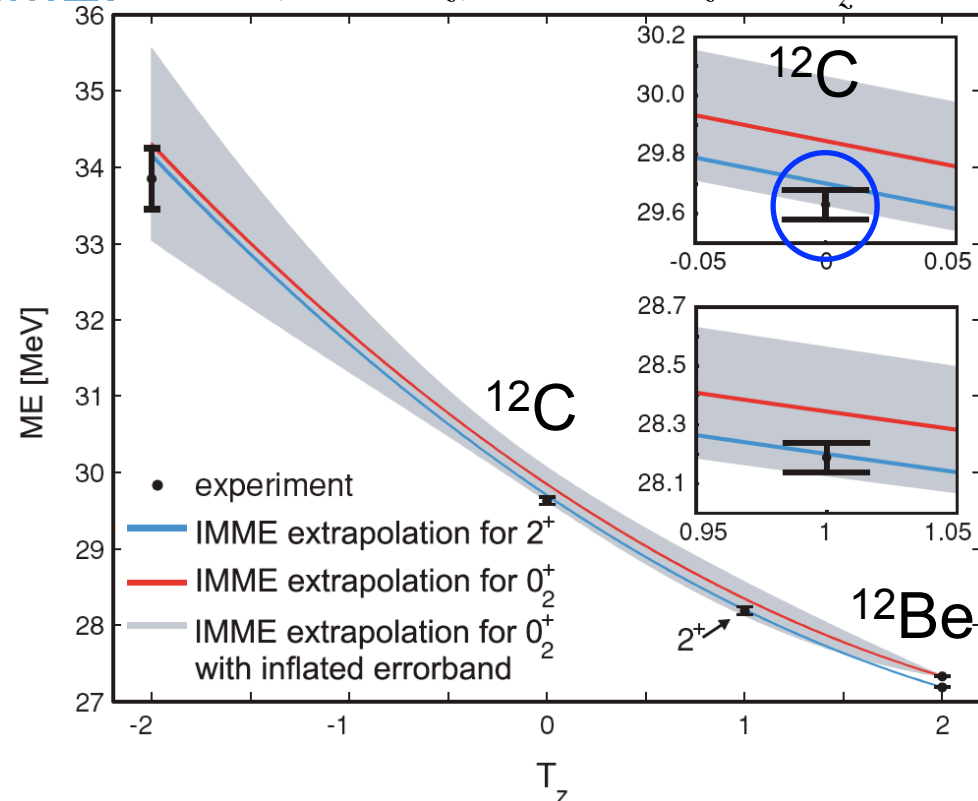
NCSM (CDB2k, INOY) r_c ^{11}Be : Forssén et al., PRC **79** (2009) 021303(R)
 FMD r_c and S_N ^{11}Be : B.R. Torobi Ph.D. thesis, Darmstadt (2010)
 NCSM (CDB2k) S_N ^{11}Be : Quaglioni et al., PRL **101** (2008) 092501

- NCSM (CDB2k): unbound ^{11}Be with a physical r_c
- Fermionic Molecular Dynamic (FMD) gives the best agreement for r_c and S_N
(potential used mimic 3 body interactions)

First step towards the mass measurement of the 2n-halo ^{14}Be ($T_{1/2} = 4.4$ ms)

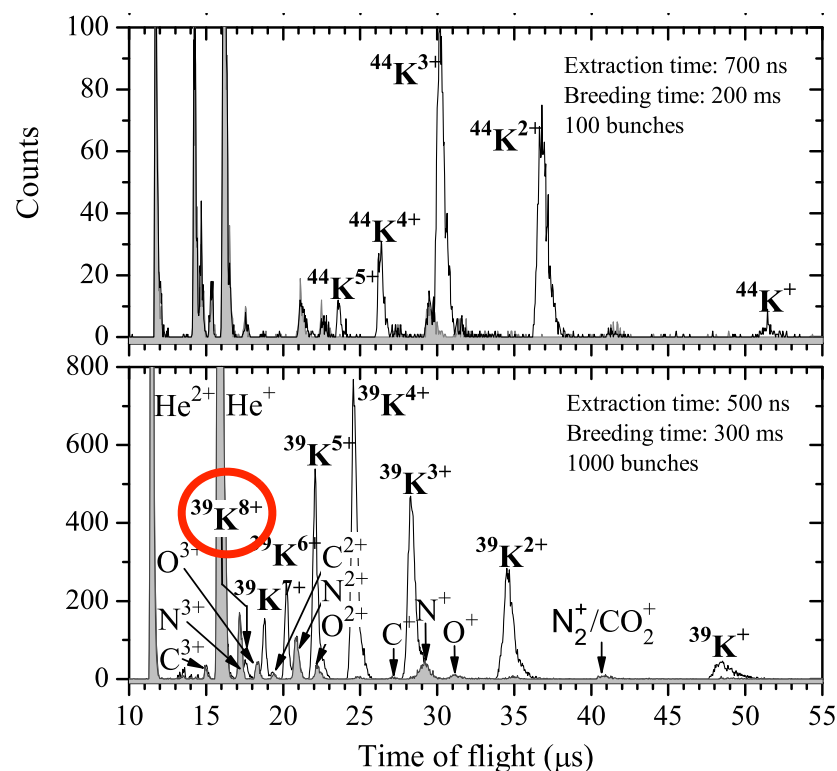


IMME: $ME(A, T, T_z) = a + bT_z + cT_z^2$

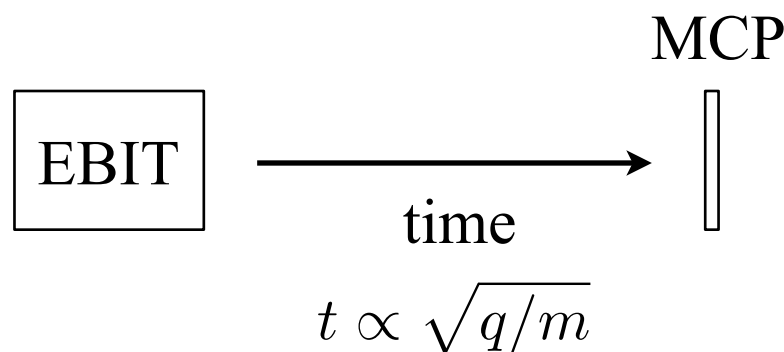


- ➔ Dispute regarding the J assignment of ^{12}C (either 0^+ or 2^+)
- ➔ Updated the $A = 12$ (for $J^p = 0^+$) IMME evaluation using the new TITAN ^{12}Be mass
- ➔ Using these fit parameters, made prediction that favours the $J^p = 0^+$ state

Time-of-flight distribution of charge bred ions from the TITAN EBIT

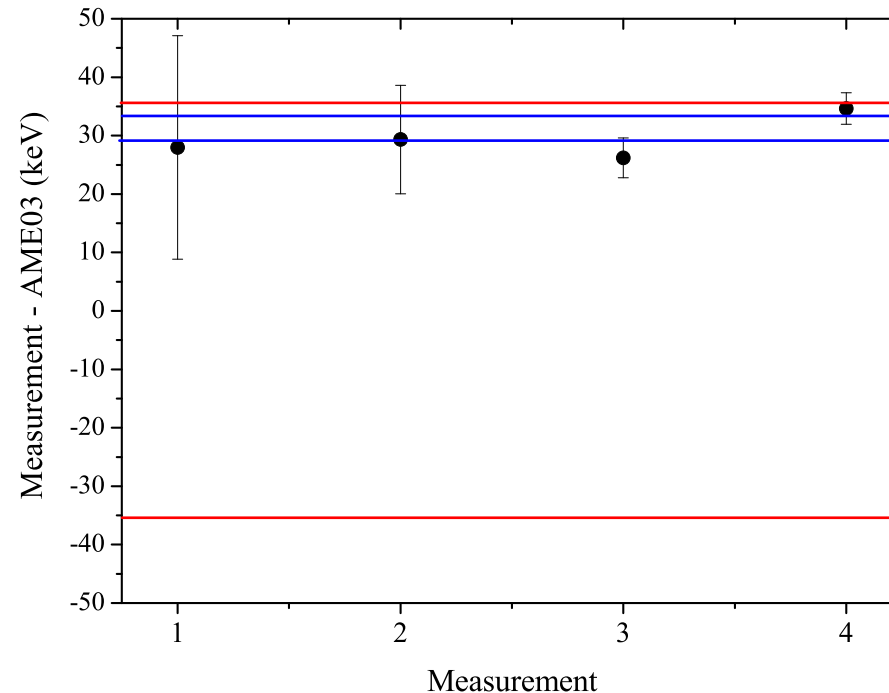
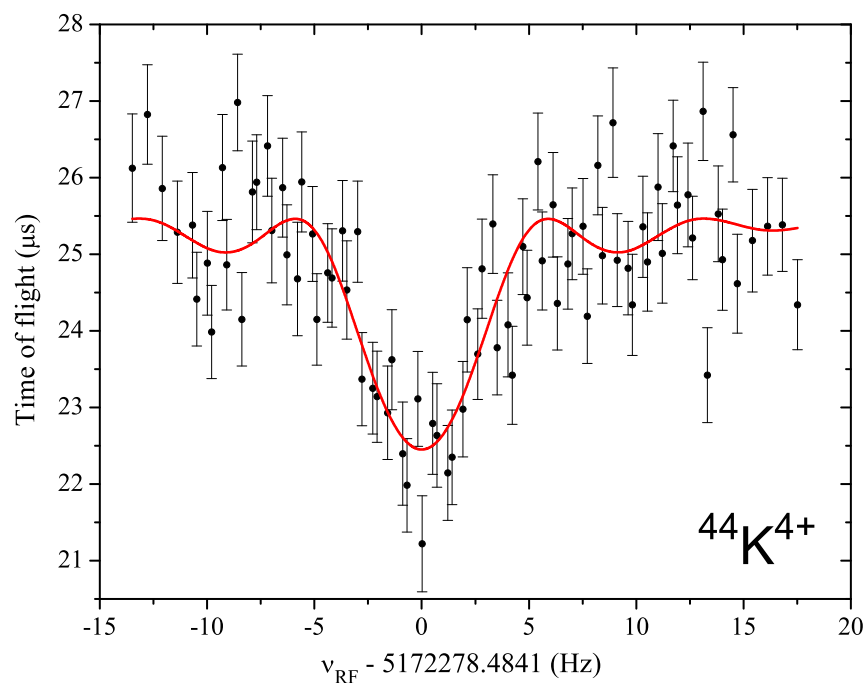


injected beam: potassium
rest: charge bred residual gas



- Observed up to 8+ charge state of ^{39}K for 2 keV e-beam energy
- Charge breeding of the residual gas (O_2 , N_2 , H_2) and ^4He from RFQ makes it presently difficult to use higher charge states of injected ions for the Penning trap.
- Total efficiency for injection/charge breeding and extraction of $^{44}\text{K}^{4+}$: 0.1%
- Charge state 4+ is not the dominant one, but the easiest to resolve from residual gas contamination

First Penning trap mass measurement using charge-bred ions: $^{44}\text{K}^{4+}$



Factor of **10 improvement** on the **AME03** mass

Future work needed for mass measurements using HCIs:

1) Improve **EBIT efficiency** for HCI production/transport

Plans: evaporative cooling in the EBIT

cooling using the cooling Penning trap (as discussed by V. Simon)

dipole cleaning in the EBIT (already demonstrated)

charge state ratio optimization

2) **vacuum** in the **Penning trap**

→ Excitation time limited to 200 ms due to Penning trap vacuum

Solution: **baked** the Penning trap (now we reached 4×10^{-11} torr)

- Accurate and precise mass measurements of halo nuclei allows to guide nuclear theory and refine our understanding of the nucleus
- Ab-initio methods points to the need of 3-body interactions in order to explain both the binding energy and charge radius of halo nuclei.
- Cluster models need to account for deformation of the core due to the presence of the halo.
- We showed that using **2 observables** involving the mass of halo nuclei, we can **test** the limitations of **nuclear theories**
- Found **deviations** of **4** and **1.7 σ** for the respective **$^{6,8}\text{He}$ masses** compared to tabulated values
- The **uncertainties** on the new **charges radii** are now **independent** of the atomic **mass**
- There are **more halo mass** measurements to come at TITAN, including **^{14}Be** and **^{19}C** .
- **Other** mass measurements are planned at TITAN, including **$^{46,48}\text{Ar}$** , **$^{51,52}\text{K}$** , and **towards ^{54}Ca** to study change in the nuclear structure

- ❖ The TITAN Group: Jens Dilling, Paul Delheij, Gerald Gwinner, Melvin Good, David Lunney, Mathew Pearson, Alain Lapierre, Ernesto Mané, Ryan Ringle, Vladimir Ryjkov, Thomas Brunner, Stephan Ettenauer, Aaron Gallant, Vanessa Simon, Mathew Smith
- ❖ TRIUMF Staff: Pierre Bricault, Ames Freidhelm, Jens Lassen, Marik Dombisky, Rolf Kietel, Don Dale, Hubert Hui, Kevin Langton, Mike McDonald, Raymond Dubé, Tim Stanford, Stuart Austin, Zlatko Bjelic, Daniel Rowbotham, Daryl Bishop
- ❖ TRIUMF Theory Group: Sonia Bacca, Achim Schwenk
- ❖ Special thanks: Gordon Drake

And the rest of the TITAN collaboration....

